Nen FAYOURITE ATH

New Favourite Math Series (Six levels) is designed in accordance with the Principles and Standards for School Mathematics (PSSM) that focus on mathematics content and its methods of teaching, and are produced by the National Council for Teachers of Mathematics (NCTM).

New Favourite Math carefully observes:

- using mathematical concepts, generalizations and laws in a smooth way.
- employing points of stimulating all forms of mathematical thinking.
- age, in addition to the developmental and physiological features of the students.
- employing modern constructivist teaching methods.
- using realistic pictures and portrayals far away from fantasy.
- · connecting mathematics with life to highlight the importance of mathematics through mathematical problems.
- designing teaching resources and aids.
- the modernity of the content and keeping up with the technological advancement.
- creating the spirit of challenge and competition.
- steering clear of routine and unnecessary repetition.









NEW



NEN FAYOURITE

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We would like to thank the editors and our designers, who all contributed to the development of New Favourite Math.

We would like to dedicate this course to the teachers around the world who will bring New Favourite Math to life in their classrooms.

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Numbers



Problem Solving

The strategies used in solving word problems:

- 1. What do you know?
- 2. What do you need to know?
- 3. Draw a diagram/picture.
- Solve the following word problems using the guess-and-check problem solving strategy to help solve math word problems.
- Make a table and look for a pattern.
- 1. Identify What is the question?

2. Plan - What strategy will I use to solve the problem?

- 3. Solve Carry out your plan.
- 4. Verify Does my answer make sense?
- Find a pattern model. Find a pattern method of problem solving strategy.
- Solving word problems:

Step 1: Identify (What is being asked?) Step 2: Write the equation(s) Step 3: Answer the question Step 4: Check



Look at the Line Number. Do you see any fractions? Do you see any mixed numbers?

1.1 Integers

A number with no fractional part is called an integer.

So, integers can be:

- Counting numbers {1, 2, 3, ...}
- Zero {0}

• Negative numbers {-1, -2, -3, ...} We can write them all down like this: {..., -3, -2, -1, 0, 1, 2, 3, ...} **Examples of integers:** -16, -3, 0, 1, 198

•Natural numbers 1, 2, 3, 4, are also called positive integers.

The Concept of Smaller and Greater Integers

The symbol $(\langle \rangle)$ means 'less than,' and the symbol (\rangle) means 'greater than'. The integers shown on the line number are written in the order of magnitude, so that the integers increase to the right. For example, 3 is to the right from 1, so it is greater than 1, and written as 3 > 1. Similarly, 0 is to the right of -2, so it is greater than -2, and written as 0 > -2. The same property of order in integers extends right across the number line of integers. The order property can be stated in a reverse manner, so that the integers decrease to the left.

As we move to the left, integers get smaller. On the other hand, when we move to the right, integers get bigger.

Exercises



- 3 Arrange the following numbers in descending order.







Fill in the blanks by using the symbols > (greater than) or < (less than). **c** -9 < -7 -18, -13, -12, -6, -2, 0, 5, 6 -9, -12, -7, 7, -16, 11, 5, -8, 16, 9, -1 16, 11, 9, 7, 5, -1, -7, -8, -9, -12, -16



1.2 Addition of Integers

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We use the number line to illustrate the addition of 3 and 4. We start at 0 and proceed three units to the right to 3. We then proceed four more units to the right; this brings us to 7. So 3 + 4 = 7



Now, let us consider the addition of negative numbers, e.g. -2 and -5. To add the negative integers -2 and -5 on the number line, we start at 0 and proceed two units to the left to -2. Then we proceed five more units to the left; this brings us to -7, (-2) + (-5) = -7



Notice that the sum of two negative integers is the negative of the sum of their numerical values, i.e.

(-2) + (-5) = -2 -5 = -(2+5) = -7

Exercise

Find the sum of the following:





1.3 Subtraction of Integers

When subtraction involves a negative number, we should learn some rules.

Consider the following examples: Subtract -2 from 6 i.e. 6 - (-2) = 8. When two negative signs (-) appear with the same number, it becomes positive. 6 - (-2) = 6 + 2 = 8.

So, when subtracting a negative number, the number becomes positive.

Find the result of the following operations:



Exercises	
(d) (-200) - (-25) =	
-175	
(f) (-14) - (-254) =	
240	
(h) 23 - 500 +120=	
-357	



1.4 Multiplication of Integers

Rule 1:

When multiplying two integers that have the SAME sign, the answer is POSITIVE.

Positive x Positive = Positive $(+7) \times (+10) = (+70)$ Negative x Negative = Positive (-5) x (-5) = (+25)

Rule 2:

When multiplying two integers that have **DIFFERENT** signs, the answer is NEGATIVE. Positive x Negative = Negative

 $(+8) \times (-6) = (-48)$

Negative x Positive = Negative

(-5) x (+7) = (-35)

Exercise

Find the product of each of the following:

a -12 X 2 = _____ -24 **b** 11 X - 11 X - 1 = <u>121</u> 200 C −20 X −10 = _____ **d** 7 X 8 X -10 = <u>-560</u> e 8 X -10 X 2 = -160 60 (f) -3 X 2 X -1 X 10 = -



1.5 Division of Integers

If both the dividend and divisor are **positive** or both are **negative**, the quotient will be positive.

Rule1: If both dividend and divisor have the same sign, positive or negative, the quotient will be positive.

 $(16) \div (4) = 4$ (positive quotient).

 $(-16) \div (-4) = 4$ (positive quotient).

Rule2: If either of the dividend or divisor is negative the quotient will be negative.

 $(16) \div (-4) = -4$ (negative quotient).

 $(-16) \div (4) = -4$ (negative quotient).

In other words (if the signs are the same, the quotient will be positive, if they are different, the quotient will be negative). This rule is for multiplication and division.

Look at this example carefully:

 $-1568 \div 13 =$ Use a calculator to find the answer. You will get -120.615. What does this mean? The answer has a decimal which indicates that the quotient is not a whole number and it's hard to solve mentally. So we need to use long division. Don't use the negative sign within the operation, but put it as the last step.







So the answer is 120 and rem = 8, but the dividend is negative, so the answer is -120 with rem = 8.





1.7 Problem Solving

- 1- Understand the problem.
- 2- Devise a plan.
- 3- Carry out the plan.
- 4- Look back.
- 1- A farmer sold 500 boxes of oranges, 1711 boxes of apples, 1202 boxes of mangoes and 777 boxes of lime. How many boxes did the farmer sell altogether?

500 + 1711 + 1202 + 777 = 4190 boxes

3.69

2- A box contains 13 rows of eggs with 14 eggs in each row. The shopkeeper rearranges the eggs in a different box, in rows of 7 How many eggs are now in each row? 26



- 4- Christmas balls arrived in a big box. The box had 48 rows, with 16 balls in each.
- a) How many balls were there altogether? 14 * 16 = 768
- b) The shopkeeper packaged boxes of balls.
 - How many boxes did she make, and how many balls were left over? SKIP
- 5- If a car moves forward, it travels a positive distance, and if it moves in reverse, metres.
- Then, it moves 8 metres in reverse. Demonstrate the car movements on a number line. use grid paper
- 6- The centigrade thermometer is marked for temperatures above the freezing point of water. Complete the marking on the thermometer below the freezing point of water.





- a) -122 ÷ -33 = ____
- 31.2 b) 36 – 24 ÷ 10 X 2 = ----
- SKIP c) 18 + X (10-12) = _____
- 51.75 d) 53 - (2 + (0.25 - 1)) = ----





it travels a negative distance. The car starts from zero (0) and moves forward 5



Fractions



2.1 The Simplification of Fractions

A fraction is described as a part of a whole. The number on the bottom of the fraction is called the **denominator**. The number on the top of the fraction is called the **numerator**. In the fraction $\frac{3}{4}$, 3 is the numerator and 4 is the denominator.

Proper Fractions (1)

Are fractions whose numerator is smaller than the denominator. $\frac{1}{2}$, $\frac{3}{4}$, $\frac{2}{5}$

Improper Fractions (2)

Are fractions whose numerator is equal to or greater than the denominator.

 $\frac{3}{3}, \frac{3}{2}, \frac{12}{5}$

Equivalent Fractions

Have the same value, even though they may look different.

We can find equivalent fractions by **multiplying** or **dividing** the numerator and the denominator of the fraction by the same number.

by multiplying:

$$\frac{1}{2} = \frac{1 \times 2}{2 \times 2} = \frac{2}{4}$$
 we see that $\frac{1}{2} = \frac{2}{4}$

by dividing:

$$\frac{6}{8} = \frac{6 \div 2}{8 \div 2} = \frac{3}{4}$$
 we see that $\frac{6}{8} = \frac{3}{4}$

Exercise

Complete the equivalent fractions.



b
$$\frac{6}{21} = \frac{18}{63}$$

d $\frac{-12}{32} = \frac{-3}{8}$

This means that there is no number, except for (1), that can be divided evenly into both the numerator and the denominator to reduce a fraction to its lowest terms. To simplify a fraction, we divide the numerator and denominator by their greatest common factor (GCF).

using the following method:

To write $\frac{20}{25}$ in its simplest form:

Find the GCF of 20 and 25. Factors of 20: 1, 2, 4, 5, 10, 20 Factors of 25 : 1, 5, 25 GCF = 5.Divide the numerator and the denominator by the GCF

 $\frac{20}{25} = \frac{20 \div 5}{25 \div 5} = \frac{4}{5}$

The simplest form of $\frac{20}{25} = \frac{4}{5}$

Exercise

Reduce the following to their simplest form.



To find a fraction in its simplest form, we can reduce it to the lowest terms

















Mixed Numbers

2.2

Numbers such as $6\frac{2}{3}$ are called mixed numbers.

To Change a Mixed Number into a Fraction

Multiply the whole number by the denominator and add the numerator to the product keeping the denominator without changing.

6.
$$\mathbf{\frac{2}{3}} = \frac{(6 \times 3) + 2}{3} = \frac{18 + 2}{3} = \frac{20}{3}$$

To Change an Improper Fraction Into a Mixed Number

Divide the numerator by the denominator. Write the remainder over the divisor.



Fractions on the Number Line

We can always find a fraction between two whole numbers by using a number line.



Exercises



2 Change the following improper fractions into mixed numbers:

<u>53</u> **a**





b $11\frac{1}{9} = \frac{67}{4}$ **d** $16\frac{3}{4} =$

b
$$\frac{25}{7} = \frac{3}{7}$$

(d)
$$\frac{36}{8} = 4 \frac{4}{8}$$





Be sure that you have the same denominator when adding and subtracting.

You may need to simplify your answer after you combine the two fractions

We just need to add the numerators 5 + 1 = 6, and the denominators







$$11 \frac{3}{4} - 5 \frac{2}{3} \qquad \textbf{d} \qquad 3 \frac{7}{10} - 2 \frac{1}{2} \\ 48 \frac{3}{4} \qquad 5 \frac{19}{21}$$

$$9 \frac{3}{8} \times 5 \frac{1}{5} = 0 7 \frac{1}{9} \times 1 \frac{15}{16} \times \frac{3}{7}$$

$$48 \frac{3}{4} 5 \frac{1}{21} = 5 \frac{19}{21}$$

c
 4
$$\frac{1}{8}$$
 d
 $\frac{15}{4}$
 $\frac{8}{33}$
 $\frac{4}{15}$

$$\begin{array}{c|c} \hline \mathbf{c} & \frac{8}{3} \div \frac{4}{5} \\ \hline \mathbf{d} & \frac{5}{8} \div 7 \\ \hline \frac{10}{3} & \frac{5}{56} \\ \end{array}$$

2.5 Property

The Distributive Property of Multiplication Over Addition

 $\frac{1}{2}\left(\frac{3}{4} + \frac{1}{4}\right) = \frac{1}{2} \times \frac{3}{4} + \frac{1}{2} \times \frac{1}{4}$

The example above shows the that multiplication is distributed over addition, in the same way the multiplication is distributed over subtraction.

e.g. Simplify $\frac{1}{4}(\frac{1}{2} + \frac{1}{3})$ using the distributive property of multiplication

over addition and subtraction.

$$\frac{1}{4} \left(\frac{1}{2} + \frac{1}{3} \right)$$

$$= \left(\frac{1}{4} \times \frac{1}{2} \right) + \left(\frac{1}{4} \times \frac{1}{3} \right)$$

$$= \frac{1}{8} + \frac{1}{12}$$

$$= \frac{3 + 2}{24}$$

$$= \frac{5}{24}$$

e.g.

 \mathbf{O}

Taking any three fractions, verify the distributive property of multiplication over subtraction.

Let the three fractions be $\frac{1}{2}$, $\frac{1}{3}$ and $\frac{1}{4}$. The distributive property of multiplication over subtraction is:

$$\frac{1}{2} \left(\frac{1}{3} - \frac{1}{4} \right)$$

$$= \frac{1}{2} \times \frac{1}{3} - \frac{1}{2} \times \frac{1}{4}$$

$$= \frac{1}{6} - \frac{1}{8}$$

$$= \frac{4 - 3}{24}$$

$$= \frac{1}{24}$$

and $\frac{1}{2}(\frac{1}{3} - \frac{1}{4})$ $=\frac{1}{2}(\frac{4-3}{12})$ $\frac{1}{2} \times \frac{1}{12}$ Hence, $\frac{1}{2}(\frac{1}{3} - \frac{1}{4}) = \frac{1}{2} x$

Exercises

subtraction.

(a)
$$\frac{2}{5} \left(\frac{3}{4} + \frac{1}{4}\right)$$

(b) $2\frac{3}{4}\left(\frac{4}{9} + \frac{1}{3}\right)$
 $\frac{77}{36}$

2 Verify the following:

a
$$\left(\frac{7}{8} - \frac{1}{2}\right) \frac{2}{3} = \frac{7}{8} \times \frac{2}{3} - \frac{1}{2}$$

This is the distributive property over subtraction.

(b)
$$\frac{3}{8} \left(\frac{2}{5} + \frac{2}{15}\right) = \frac{3}{8} \frac{2}{5} + \frac{3}{8}$$

This is the distributive property over addition.



$$\frac{1}{3} - \frac{1}{2} \times \frac{1}{4}$$

1 Simplify by using the distributive property of multiplication over addition or

$$x \frac{2}{3}$$

$$x \frac{2}{15}$$

 $\frac{2}{5} = \frac{2 \times 2}{5 \times 2} = \frac{4}{10} = 0.4$

Operations With Decimals 2.6

Decimals are a simple way of writing fractions whose denominator is a power of 10.



The dot (.) is called the decimal point.

Note: The number of digits to the right of the decimal point is equal to the number of zeros in the denominator of the given fraction.

The numbers to the left of the decimal point represent whole numbers. The numbers to the right of the decimal point represent fractions. The chart below shows the place value of digits to the right of the decimal point:

Note: Each place has a value of $\frac{1}{10}$ to that of the place to its left.

```
Decimal Equivalents
```

Tenths	$\frac{1}{10} = 0.1$	Hundredths	$\frac{1}{100} = 0.01$
Thousandths	$\frac{1}{1000} = 0.001$	Ten thousandths	$\frac{1}{10,000} = 0.0001$

To read .01 we say one-hundredths or point zero one.

1- Addition and Subtraction of Decimals

To add (or subtract) decimals follow these steps.

- (1) Write the given numbers one above the other with the decimal points in a vertical line.
- 2 Add or subtract the numbers as needed.
- 3 Write the sum or difference.

e.g. Add 21.783 + 1.92 + 32	.1
21.783 1.920 <u>+ 32.100</u> 55.803	
1 Copy to your textbook then ac	d o
a 46.342 +15.296 61.638	
c 24.37 – 18.26 6.11	(
e 15.003 - 14.386 0.617	(
2 Copy to your textbook then sir	npl
a 75.2 + 18.6 - 65.3 28.5	(
2- Multiplication of Decimals	
A- Multiplying by10, 100 and 1000	(Po
Steps: O	
- Move the decimal point to th zeros in the fraction.	ie r
- Move the decimal point two	ste
$32.24 \times 10 = \longrightarrow 32.24$	
The decimal shifts 1 place to the	ne

e.g. Subtract 18.71 - 0.3 18.71 <u>- 0.30</u> 18.41
or subtract the following.
b 129.235 + 16.41 <u>145.645</u>
d 76.423 – 38.9 37.523
f 49 - 3.276 45.724
lify and find the answer.
b 39 - 16.28 + 15.75 38.47
owers of 10)
right as many places as there are
ep to the right (10 has one zero). eps to the right (100 has two zeros).

322.4

right.





To Chec	ck				
15.48	÷	4	=	3.87	
(divider	nd)	(diviso	r)	(quotien	†)
Multiply The pro	the c	quotient will be tl	by t he d	he diviso ividend.	r.
3.87	Х	4	= '	15.48	

When dividing by 10, move the decimal point one place to the left.



Converting Between Fractions and Decimals

.25		
<u>1,0</u>		
- 8		
20		
0		

<u>45</u>	e <u>24</u>	f <u>11</u>	g <u>6</u>
200	25	20	13
<u>19</u> 20			

decimal point. (For example, if there are two numbers after the decimal



eg Witte down 0.75:

$$\frac{9.75}{1} \\
\frac{9.75}{1 \times 100} = \frac{75}{100} \\
\frac{75}{10} \quad 15 = \frac{15}{10} \quad 3 = \frac{3}{4}$$
eg Change the following decimal fractions into common fractions:
(a) $1.5 = 1 \frac{5}{10} = \frac{15}{10} = \frac{3}{2} \quad 1.5 = \frac{3}{2}$
(b) $0.25 = \frac{25}{100} = \frac{1}{4}$
(c) $3.25 = 3 \frac{25}{100} = \frac{325}{100} = \frac{13}{4} = 3 \frac{1}{4}$
Exercises
(1) Convert the following into fractions.
(a) $0.3 \frac{3}{10}$ (b) $0.75 \frac{3}{4}$ (c) $6.25 \frac{1}{4}$ (d) $0.25 \frac{1}{4}$
(e) $1.875 1\frac{7}{8}$ (f) $0.0005 \frac{1}{2000}$ (g) $0.075 \frac{3}{40}$ (h) $0.675 \frac{27}{40}$
(2) Withe each of the following as a decimal fraction.
(a) 1 tenth 0.1 (b) 5 hundredths 0.05 (c) 3 thousandths 0.003
(3) Arrange in descending order.
(a) $-1.37, -1.74, -1.26, -1.093$ (b) $\frac{4}{5}, -\frac{5}{8}, 0.75, 0.66, 415, 0.75, 0.66, 518 -1.093, -1.23, -1.37, -1.74$
(c) $0.33, 0.23, 0.04, 0.008$ (b) $\frac{3}{-16}, -0.281, -0.099, \frac{1}{-8} -0.281, 3.416, 1/-8, -0.099$

Uses of Brackets Involving Arithmetic Operations

BODMAS :



2.8 **Problem Solving**

- 1- Understand the problem.
- 2- Devise a plan.
- 3- Carry out the plan.
- 4- Look back.

 \bigcirc

- Solve the following word problems.
- 1- There is 0.625 kg of powdered milk in each tin. If a carton contains 12 tins, find the total mass of powdered milk in the carton. 0.625 * 12 = 7.5
- 2- The mass of a jar of sweets is 1.6 kg. What is the total mass of 8 such jars of sweets? 1.6 * 8 = 12.8
- 3- Carpeting costs \$9.99 a yard. If Jane buys 17.2 yards, how much will it cost her? (Round your answer to the nearest hundredth)9.99 * 17.2 = 171.83
- 4- Order from least to greatest: $\frac{8}{9}$, $\frac{17}{18}$, $\frac{2}{3}$, $\frac{7}{6}$, 2/3, 8/9, 17/18, 7/6
- 5- What fraction of 1 hour is 50 minutes?

Algebra is a branch of mathematics that deals with symbols. In elementary algebra, those symbols are written as Latin and Greek letters representing quantities without fixed value, and they're known as variables.

Who first founded algebra?

Review

The order of operations is:

- 1- Simplify the expressions inside parentheses () and brackets [].
- 2- Evaluate all powers.
- 3- Do all multiplications and divisions from left to right.
- 4- Do all additions and subtractions from left to right.



We have to do the multiplication first. Then, we continue with subtracting 32 - 2 to get 30.

Exercise

Simplify the following expressions:

- (a) $(2 + 3) \times (7 3)^2 = 80$
- (c) 36 + 15 (40 35) = 111





b
$$4 + 5 \times \frac{3}{5} = 7$$

d
$$2 \times ((8 - 3)^2 + 6 \times 2) = 74$$





3.1 **Algebraic Expressions**

An algebraic expression is the combination of variables, constants, coefficients, exponents, and terms which are combined together by the following arithmetic operations: addition, subtraction, multiplication, and division. An example is given below:

3x + 7y - 10. Read it and give another example.

Variables: Alphabetical charcters which are used for assigning the value. Widely used variables are x, y, t, k

Constant: Algebraic constants have values that never change like

2, 15, <u>-2</u>

Term: Term of the algebraic expression is concatenated to form the algebraic expression by arithmetic operations such as addition, subtraction, multiplication and division. For example:

2x + 10

The number that multiplies by a variable is generally written in front it. For example:

2x, the coefficient is 2.

When the coefficient equals 1, it is usually is not written.

(i.e. ? |xy = xy, x = | x x).

Exercise: Complete the following table.

Algebraic expression	Number of terms	Terms	Variables	Coefficient
2x + 9	2	2 <i>x</i>	x	2
		9		
$2x^2 + 3y + 7$	3	$2x^2$	х,у	2, 3
2		Зу 7		
$7x^2 - 12by^2$	2	7x ² , 12by ²	x, by	7, 12
$\frac{9}{12} + \frac{7b^2x}{8} - 3y$		9/12, 7b ² x/8, 3y	b, x, y	

In other words:

A variable is a letter used to represent a value that can change. X

A constant is a value that does not change. 9

A numerical expression contains only constants and operations. 2 + 9

An algebraic expression may contain variables and constants. **2***x* **+ 9**







Combining Like Terms 3.2

Simplify an expression by combining like terms. For example 3a + 6b - a + 3b.

Combine the like terms 3a, (-a) to get 3a + (-a) = 2a and combine the like terms 6b, 3b to get 6b + 3b = 9b.

Then 3a + 6b - a + 3b is simplified to 2a + 9b.

e.g. a
$$10k^2 + 15k^2 = 25k^2$$

b 7xy - 6xy + 7x = xy + 7x

Algebraic expressions	Simplest form
3t+12y-t+10a-10t+5y+t	10 <i>a</i> -7 <i>t</i> +17y
$7x^2 + y^2 - 6x^2 + y$	$x^2 + 2y$
xy + 3x + 2y + xy - x - y	2xy + 2x +y
$14b - 2b^2 + 4b$	18b - 2b ²
26+5h - 10+12k -5b-12k-6	<u>10 + 5h - 5b</u>
$25t^{3} + 14t^{3} - 8d^{2} - 10 + 2d^{3}$	$\frac{39t^2 - 8d^2 - b + 2d^3}{2}$

Complete the following table.

Do you notice that:

 $x+y \neq xy$

 $x+y \neq 2x \text{ or } 2y$

 $x^2 + x \neq x^3$ or 2 x^2 or 2x or 2 x^3

Exercises

1- Simplify the following expressions.

- 1 10y 12y + 6 = 6 2y
- **3** $9t^2 7t + 4 2t^2 + 5t = 7t^2 2t + 4$

2
$$2x^2 - 3x - 2x^2 = -3x$$

4
$$3xy + 3(xy + z) = 6xy + 3z$$

Remember, distributive priority: a(b + c) = ab + ac

2- Simplify the following expressions. - The expression for the operation descri

a) x multiplied by 5 is: 5x

b) x plus 5 is: x + 5

c) 3 times v is: $\frac{3v}{2}$

- d) The sum of v and x is: v + x
- e) 6 divided by 6 is: _____1
- f) The quotient of 4 and x is: —

g) 4 decreased by y is: 4 - y

h) 6 increased by g is: 6+g

i) Raise 3 to x then multiply f by the resu

3- Write an expression that represents the

a) John ate x out of 34 cookies: _____

b) Sara bought 19 chocolates, Mike bo

as Sara, write an expression that show

Sara bought: ____

c) Paul has x red peppers and 20 green peppers, write an expression

that shows how many peppers Paul has: ____ X + 20



ibed:
e statement of the following:
34 - X
bught x times as many chocolates
ws how many chocolates
SKIP





Evaluating mostly means simplifying an expression down to a single numerical value.

1

Evaluate each expression when: $x = 2, y = 1, z = 0, m = \frac{1}{2}$

$$1 \quad 2x + 3yz = 2 (2) + 3 (1) (0) \longrightarrow 4 + 0 = 4.$$

2
$$x^{2} + 2y - 2m = (2)^{2} + 2(1) + 2(\frac{1}{2}) \longrightarrow \frac{7}{7}$$

3
$$xy - 3z - xm = (2)(1) - 3(0) + 2(\frac{1}{2}) \longrightarrow$$

To evaluate a variable expression:

- 1) Substitute the given numbers for each variable.
- 2 Use the order of operations to evaluate the algebraic expression.
- 3 Check!

Exercise

1- Find the value of the following: (15b - 5x) + 2(4b) + 3 = for b = -1, x = 2lst step: (15(-1) - 5(2)) + 2(4(-1)) + 3 =2nd step: (-15-10) + 2(-4) + 3 = (-25) + (-8) + 3 = (-33) + 3 =30 Check it by calculator, is it right?



j
$$2 \times (x + 2)$$
 for $x =$



-2

Equations and Inequations



4.1 The Equation

Look at these number sentences:

Write (T) when the statement is true, and (F) when the statement is false.



What do you notice?

Lets' take 20 + 5 = 30 - 5 We have two equal sides.

Left side Right side



The Equation

is a statement that two things (expressions) are equal. For example the (expression) 20 + 5 is equal to the (expression) 30 - 5(because they both equal 25).

Let's make sure we know the difference between an expression and an equation.

Which of these is an equation? (Put \checkmark).



Most equations include a variable. For example, x + 3 = 4 has a variable (x) If an equation contains a variable, it's called an algebraic equation. For example: x + 3 = 4 has a variable, which is x.

An equation introduces two equal things.

$\chi + 3 = 4$

That equation says: What is on the left (x + 3) is equal to what is on the right (4). So, an equation is like a statement of "this equals that".

If we substitute x for 0,

we get $0+3 \neq 4$, 3 doesn't equal 4, so $x \neq 0$ Lets try x = 1

1+3 = 4. It is a true statement. Can you find more solutions?

Exercises

Choose the answer that makes the equation true. 1 7 + x = 12. So x =(a) 2 = 10 (b) $\chi = 9$ (2) 1 + y = 20. So y =**a** y = 10 **b** y = 1 3 2(x) = 20. So x =**(b)** x = 2(a) x = 10







Solving One-Step Equations 4.2

You have already studied equations where the solutions were quite easy to solve by using mental math or patterns, most equations are harder to solve mentally, so they need simplifying before you can get the solution. One way to do this is by:

7x + 3x

1

Using Inverse Operations

The inverse operation of addition is subtraction, and the inverse operation of subtraction is addition.

So: X + 4 =22

We have to subtract 4 from both sides.

x + 4 = 22

 \bigcirc

-4 -4

x = 22 - 4x = 18Then, check your answer: ls (18) + 4 = 22 ? $22 = 22 \checkmark$ So the answer is right.

Otherwise, an inverse operation is an operation that reverses the effect of another operation.

Addition and subtraction are inverse operations.

Division and multiplication are inverse operations too.

Find the value of y in: 2y = 10

Notice that the operation between 2 and y is multiplication, so the inverse operation is division. Then, divide both sides by 2.

 $\frac{2y}{2} = \frac{10}{2}$ $y = \frac{10}{2}$ = 5

→ 5 (5) = 10 Check -10 = 10

Exercise



$$6z = 6$$
$$z = 1$$

$$\frac{m}{11} = 7$$
$$m = 77$$

$$4g = 8 + 12$$

g = 5

b
$$6.3 = v + 2$$

 $v = 4.3$

$$\begin{array}{c} \mathbf{j} \quad x - \frac{1}{2} = \frac{3}{4} \\ \mathbf{x} = \frac{5}{4} \end{array}$$





- (d) x + 4 > 12, x = 13 (T).
- (f) $2y 7 \le 14$, y = (10) (T).

C
$$4 \times 1$$

Before you answer, read the next note.
C 4×1
Before you answer, read the next note.
C 4×1
 4×1

Note: Use a closed dot (•) to indicate the number itself is part of the solution with \leq and \geq . Use an open circle () to indicate the number itself is not part of solution with < and >.

- 2-Write the following inequalities through symbols and give examples of solutions.
- (a) A number decreased by 2 is greater than or equals 5. $x 2 \ge 5$
- **(b)** Twice a number decreased by 4 is greater than 8. 2x 4 > 8
- C Half a certain number increased by 5 is less than ten. $\frac{x}{2} + 5 < 10$
- 3- Solve the following inequalities:
- **a** 5x 2 < 8 **x < 2**
- **b** $x + 7 < 9 \times < 2$
- **c** x + 7 < 9 skip



Problem Solving

- 1- Understand the problem.
- 2- Devise a plan.
- 3- Carry out the plan.
- 4- Look back.
- 1- Sara bought y sweets, she gave 4 sweets to her sister. (a) How many sweets does she have now? y - 4(b) If she now has 8 sweets, write an equation and use it to find the value of (y)
- 2- There are (x) apples on the table. The children ate 6 of them.

(g) How many apples are left? x - 6(b) If (x) apples are left, write an equation and use it to find what number (x) stands for. skip

3- Louis weighs (k) kilograms and his father weighs 70 kilograms.

(a) What is their total weight? y = k + 70

(b) If their total weight is 100 kilograms write an equation and use it to find the value of (k). k + 70 = 100k = 30

- 4- Write an equation for each of the following and solve it.
 - (a) 12 less than x equals 15. $\begin{array}{c} x 12 = 15 \\ x = 27 \end{array}$ (b) 7 more than x equals 25. x + 7 = 25
 - x = 18
 - (c) Add 11 to \hat{k} and the answer is 20. k + 11 = 20

(d) A father is 40 years old, his daughter is x years old, their total age is 52 years.

x + 40 = 52x = 8









Ratio and Proportion

5- Lee answered all the questions on his math test but got 10 answers wrong.

He received 4 points for every correct answer, and there was no penalty

for wrong answers.

His score was 76 points.

Write an equation to determine the total number of questions (q) on Tim's math test.



5.1 Ratios

The comparison by division of two quantities in the same unit is a ratio. The ratio of 2 to 3, is denoted by 2:3 (is read 2 to 3)

and is measured by a fraction $(\frac{2}{3})$.

1) The speed of a car is 60 kilometers per hour and the speed of a bus is 45 kilometers per hour. The ratio of their speed is 60 : 45

 $=\frac{60}{45}=\frac{4}{5}$ How can you read this ratio ?

2 The price of a banana ice cream and a mango ice cream is \$2 and \$3 respectively. The ratio of their price is = 2 : 3

 $=\frac{2}{3}$

Can you get the price of the banana ice cream if the mango ice cream is priced as \$9?

Simplify the ratio:

$\frac{2}{4}$: $\frac{5}{6}$	
$=\frac{2}{4} \times \frac{6}{5} = \frac{12^{3}}{20^{5}}$	Ratios sh possible.
$=\frac{3}{5}=3:5$	A ratio is (or quan
or 2 x 6 : 4 x 5	and divid
= 12 : 20	
$=\frac{12}{20}=\frac{3}{5}=3:5$	







atios should be expressed as simply as

ratio is unchanged if the two numbers or quantities) of the ratio are multiplied nd divided by the same number.







The ratio between Sami's and Sonny's shares is 2 : 3 and that between Sonny's and Dani's shares is 3 : 4. What is the ratio between the shares

rrange the ratios as shown below.				
ny's share	:	Dani's share		
3				
3	:	4		

3 4 Thus, the ratio of the shares of Sami and Dani is 2 : 4 or 1 : 2 (simplified form). This type of comparison is called comparing with the help of

In the example above, Sonny's share is 3 in both ratios. i.e Sonny's

Now we will take an example where the common share is not the

The ratio in the ages of A and B is 3: 4 and of B and C is 5: 7. Here B is common to both the ratios. Arrange the ratios as shown below, and then multiply as indicated by the arrows to get the continued ratio.





The ratio in the income of A and B is 2:3, and of B and C is 4:5 and of C and D is 6 : 5 Find the ratio between the incomes of A, B, C and D.



Note: In order to reduce the ratio to its simplest form, each number is divided by the common factor.

Exercises

- 1) Find the continued ratio between A, B and C when A : B is 4 : 5 and B : C is 5 : 6. 20: 25:30
- 2 The ratio between the marks obtained by Ali and Jake is 2 : 3 James and Alfred is 5 : 6 while Frank and Shane is 3 : 4 . Find the ratio between the marks obtained by James and Shane. 72
- 3) 1) A : B = 3 : 5, B : C = 3 : 4 and C : D = 5 : 6 Find A : B : C : D in the simplest form, 9:15:20:242) A : B = 20 : 27, B : C = 8 : 15, C : D = 5 : 6. Find A : B : C : D 100 : 216 : 405 : 486
- 4 The ratio in the shares of A and B is 5 : 11, B and C is 4 : 5 and C and D is 7: 8. Find the continued ratio among A, B, C and D. 140: 308: 385: 440

Proportional Division 5.3

Suppose a stick is cut into three pieces - A, B and C- such that A is 6 cm long, B is 9 cm long and C is 12 cm long. We can then say that the ratio of the length of A to the length of B is 6 : 9 or 2 : 3 and the ratio of the length of B to the length of C is 9 : 12 or 3 : 4. We can also say that the stick is cut into pieces in the proportion 2 : 3 : 4. We can write: length A: length B: length C = 2:3:4

This means that the length of A = $\frac{2}{3}$ of the length of B. The length of A = $\frac{2}{4}$ or $\frac{1}{2}$ of the length of C. The length of $B = \frac{3}{4}$ of the length of C. The length of B = $\frac{3}{9}$ or $\frac{1}{3}$ of the original length of the stick. The length of A = $\frac{2}{2}$ of the original length of the stick.

To divide a certain quantity in a given ratio is called proportional division.

.g.	Divide\$1500 among	Fara
	Amount	=
	Ratio	=
	Sum of ratios	=
	Farah's share	=
		=
		=
	Lara's share	=
		=
	Sara's share	=
		=
	Therefore,	
	Farah's share	=
	Lara's share	=
	And Sara's share	=

```
ah, Lara and Sara in the ratio of 3:4:5
  $1500
  3:4:5
  3 + 4 + 5 = 12
    ratio
               x amount
  sum of ratios
  \frac{3}{12} \times 1500
 $375
     x 1500
 $500
  <u>5</u> x 1500
 $625
  $375
  $500
  $625
53
```

ratio sum of ratios Note: Each Share = x Amount

Application to Partnership and Profit Sharing

When two or more people invest in a business, the profit obtained is divided according to their respective investments, the ratio of profit will be the same as the ratio of the investments. If two people invest equally, the profit will be divided equally. If two people invest in the ratios of 1 then it will be divided in the ratios of 1:2.

Exercise

Divide \$9100 among Ali, Sami and Hillary in the ratio 2 : 4 : 7

Sara invests \$100,000 in a business and Selena invests \$200,000. At the end of the year, the profit is \$9,000. What will their respective shares in the profit be? Ali = (2/13) * 9100 = 1400Sami = (4/13) * 9100 = 2800

Sarah's investment \$100,000	Hillary = (7	7/13)	* 91	90 <u>= 4900</u> Selena's ii \$200,000	nvestment
Ratio of investment		1	:	2	
Ratio of profit		1	:	2	
Sum of ratios	= 1 + 2 =	3			
Profit per unit ratio					<u>9,000</u>
(Is one part of the prof	fit out of 3):				3
Sara's share	=		<u>9,00</u> 3	<u>00</u> x 1	= 3,000
Selena's share	=		<u>9,00</u> 3	<u>00</u> x 2	= 6,000

Sami, Sonny and Dani invest in a business, \$500,000, \$400,000 and \$300,000 respectively. They earn a profit of \$18,000. Find the shares of each partner. Ratio of investment:

Sami	:	Sonny	:	Dani
\$500,000	:	\$400,000	:	\$300,000
5	:	4	:	3
Sum of ratios	:		5	5 + 4 + 3 = 1

Profit per unit ratio (that is, one part of the profit out of 12): 18,000 12

Sami's share $=\frac{18,000}{12} \times 5 = $7,500$ Sonny's share $=\frac{18,000}{12} \times 4 = $6,000$ Dani's share $=\frac{18,000}{12} \times 3 = $4,500$

Exercises

- 1 A class has 30 girls, two-thirds have long hair. Find the number of girls with long hair. $20 = (30/3 \times 2)$
- 2 A boy has \$60 pocket money, he spent two-thirds of it. What amount did he spend? 60/3 * 2 = 210
- 3 Three fishermen caught 1,380 fishes. If the ratio between their fish is 8:9:6 How many fish did each of them catch?
- a \$100 in the ratio 2 : 3

 $100/5 \times 2 = 40$ (Selena) 100/5 * 3 = 60 (Linda)

2



4 Divide the given amount between Selena and Linda in the given ratios:

(b) \$4,500 in the ratio $\frac{1}{5}$: $\frac{1}{4}$

S.O.R = 0.94500/0.9 * 0.5 = 2500 (Selena) 4500/0.9 * 0.21 = 2000 (Linda)

Direct Proportion 5.4

An expression of equality between two ratios is called a 'proportion'. The ratios 2:3 and 4:6 are equal, hence, 2:3 = 4:6. This may also be written as

2:3::4:6

Look at this example:

Sami earns \$20 and saves \$5. Sara earns \$16 and saves \$4.

 $\frac{5}{20}$

Since

$$= \frac{1}{4} \text{ and } \frac{4}{16} = \frac{1}{4}$$
$$\frac{5}{20} = \frac{4}{16}$$

So the two ratios are equal.

The above proportions may also be written as:

5:20::4:16

It is read as 5 is to 20 as 4 is to 16.

The four numbers used in a proportion are the terms of the proportion. In the above proportion, 5 is the first term, 20 is the second term, 4 is the third

term and 16 is the fourth term.

The second and third terms are called the means. The first and the last terms are called extremes.

In the proportion 5:20 = 4:16, the 20 and the 4 are means and they are also called 2nd and 3rd proportions while the 5 and 16 are extremes, and also called 1st and 4th proportions.

In any proportion the product of means equals the product of extremes.

In the proportion 5:20 = 4:16

 $5 \times 16 = 80$ Product of extremes

 $20 \times 4 = 80$ Product of means

If three terms of a proportion are known, the missing term can be found.



2:4 and 1:2 ls it a proportion? 2:4:1:2

So, yes, it is a proportion.

A 30-cm-long piece of string costs \$5. What is the cost of a 45-cm-long string.



Note: All the examples given above are examples of direct proportions. directly on the other.

In the unitary method, we find first the value of a unit and then multiply that with the number of units given.

Unitary Method

e.a.

The cost of 6 pens is \$42. Find the cost of 13 pens.

- The cost of 6 pens is \$42 The cost of 1 pen is \$42
- The cost of 13 pens is $\frac{$42 \times 13}{6}$ = \$91
- Note: The unitary method is possible only when two quantities are in direct proportion. direct proportion.



: : 5 : 30

In a direct proportion, two quantities are related in such a way that if one increases, the other also increases, and if one decreases, the other decreases. In a direct proportion, one quantity depends

Hence, we can say that the unitary method is a special case of



Consider some examples on the unitary method. If. 2 balls cost \$8, find the cost of 3 balls.

Cost of 2 balls = \$8

Cost of 1 ball = $\$8 \div 2 = \4

Cost of 3 balls = $4 \times 3 = 12$

Exercises

(1) 12 toys cost \$72. Find the cost of 4 toys? $72/12 \times 4 = 24

- ² If 6 pens cost \$96, how much would each pen cost? And how much would 18 pens cost? 96/6 = \$16 16 * 18 = 2
- 3 If the cost of 8 chocolate bars is 16. Find the cost of 17 chocolate bars.

16/8 * 17 = 34



Indirect (Inverse Proportion)

Inverse proportion or indirect proportion: is a relation between two guantities such that one increases in proportion as the other decreases, or the other way round.

For example, if a particular job requires 4 men to complete it in 8 hours, then the same job will require 8 workers to perform it in 4 hours. Here the number of workers and the number of hours are in inverse proportion.

Three men can complete a work in 4 hours, how many men will do the iob in 12 hours?

As a direct proportion, this ratio would have been 3: x = 4: 12but this proportion is an example of inverse proportion, therefore, the ratio should be shown in the following way. x: 3 = 4: 12

And the product of means

Ixample



Find the 4th proportion of the followin



Now the product of extremes = 12 x= 3 x 4 $12 x = 3 \times 4$ $x = 3 \times 4$ 12 x = 1 man

> The product of means = 3 x 10 = <u>3 x 10</u> = 15

ng ratio:	6 : 8 : : [18 : 24
ng ratio:	6:9::3	30 : 45

5.6 Percentage

Percentage is used in many fields such as, business, sports and others. It is a way to show how each quantity is related to another. Percentage means hundredths, we use the symbol % which is read as percent. In a common fraction, like $\frac{2}{2}$, we have a numerator and any number as a denominator. A percentage is a special fraction with only one denominator (100). Hence, 50% 50 percent) means $\frac{50}{100}$ or $\frac{1}{2}$. Conversely, a fraction can be changed to a percentage as follows: $\frac{3}{4}$. This is a common fraction with a denominator of 4. In percentage, the denominator must be 100. So, the change of $\frac{3}{4}$ to percentage will require changing the denominator to 100.

$$\frac{3}{4} = \frac{3 \times 25}{4 \times 25} = \frac{75}{100} = 75\%$$

Rules: To express a percentage as a fraction divide it by 100.

Express 12 percent as a fraction.

$$12 = \frac{12}{100} = \frac{3}{25}$$

2 Express 12 $\frac{1}{2}$ percent as a fraction. $12\frac{1}{2} = \frac{25}{2} = \frac{25}{2} \div 100 = \frac{25}{2} \times \frac{1}{100} = \frac{1}{8}$

3 Express 25 percent as a decimal fraction.

$$25 = \frac{25}{100} = 0.25$$

Note: When a number is divided by 100 the decimal point is shifted towards the left by two places.

- Express $2\frac{1}{2}$ percent as a decimal fraction.
 - $2\frac{1}{2} = \frac{5}{2} = 2.5 = \frac{2.5}{100} = 0.025$

Note: When there is only one number before the decimal point, then a zero is added on the left and the decimal point is placed before the zero.

Note: To express a fraction as a percentage, multiply it by 100.

5 Express $\frac{3}{4}$ as a percentage.

```
\frac{3}{4} = \frac{3}{4} \times 100 = \frac{300}{4} = 75\%
```

Express 0.06 as a percentage. 6 $0.06 = 0.06 \times 100 = 6\%$

Note: When a number is multiplied by 100, the decimal point is moved two places to the right.

- Note: To find the percentage of a given quantity, multiply the quantity by a
 - Find 40 percent of \$300. (7)

40% of \$300 = $\frac{40}{100}$ x 300 = \$120

25 percent of a number is 50. Fi



fraction whose numerator is the given rate and whose denominator is 100.

nd the number. 25% of x = 50

$$\frac{25}{100} x = 50$$

$$x = \frac{5 \times 100}{25}$$

$$x = 200$$
Thus, the number is 200.





Leen makes money by commission rates, she gets 10% of everything she sells, if she sold 25000 this month, what is her salary for the month?

Sue earns a 5% commission on each mobile she sells, if each mobile costs \$200, and she sells 31 mobiles to the mobile store, how much commission

5.8 Discount

A discount means a reduction in price. It is the percentage that is subtracted from a number. For example, a 10% discount of \$300 is \$30. So, if an item that sells for \$300 is offered at a 10% discount, it can be bought for \$270.

On a clearance sale, the price of a computer was reduced from \$500 to \$450. Find the discount percent.

Original price	= \$500	ACCOUNT
Reduced price	= \$450	c0°/o DISOCONT + + +
Discount	= original price - reduced price	
	= 500 - 450	
	= \$50	
Discount %	$= \frac{\text{Discount}}{\text{Original Price}} \times 100$	
	$= \frac{50}{500} \times 100$	DISCOUNT
	= 10	3
Thus, discount	= 10%	Pole DISCOUNT * *

Example

The written price of an article is \$250. A discount of 10% is given. Find the discount and the reduced price of the article.

Original price	= \$250
Discount	= 10% of \$250
	$=\frac{10}{100} \times 250$
	= 25
Reduced price	= Original price – discount
	= 250 - 25
	= 225
Thus, discount	= \$25
and reduced price	= \$225
	\frown

Exercises 1) Find the sale price of an item that has a list price of \$24 and a discount rate of 50%, $24 \times 0.5 = \$ 12$ Test whether the following proportions are true or false. **a** 4 : 6 :: 3 : 2 **d** $\frac{1}{5}$:: 5 : 4 F 3 Fill in the :6::2:3 (a) 4 (b) If 5 apples cost \$30, what will be the cost of 9 apples? 30/5*9 = \$545 6 Two dozens of pens cost \$72. Find the cost of 50 pens. SKIP A car covers a distance of 180 km in 3 hours. What distance will it cover in 7 hours travelling at the same speed? The weekly expenditure of a family is \$840. Find their expenditure for a month (30 days). 840 * 30 / 7 = \$ 3600 The wages of a manger are \$150 per day. Find his income for (i)..... 9 skip (ii) (10)If (25) computers cost \$12,500. Find the cost of (35) computers. 12500 * 35/25 = 17500

8:6::4:3 Т $\frac{2}{4}:\frac{3}{5}::5:6$ T

9 : 27 : : 3 : 9

A tree grows in 5 months by 62 cm. What will be its growth after 9 months? $\frac{5}{62} \times \frac{9}{X} = 111.6$

3/180 = 7/x= 420 km

If 39 men earn \$2340 in a day's work, what would 91 men earn in a day? 2340 * 91 / 39 = \$5460







By covering 20 km a man has covered 25 percent of his journey (7) What is the total length of his journey? y = 20 * 100/25 = 80







```
80 = 2 * 8 + 2L
```







Perimeter and Area of Triangles 6.3

The perimeter of a triangle equals the sum of the lengths of its three sides.



So, to find the perimeter of the triangle abc bellow:



The area of a triangle = $\frac{1}{2}$ x Base x Height

The height of a triangle is each of the perpendicular lines drawn from one vertex to the opposite side.









6.4

Perimeter & Area of Parallelograms & Trapezoids

We learned that the perimeter is the distance around a two-dimensional closed shape, or it is the length of the boundary. Find the perimeter of the shapes below:



6.5 Volume of Cubes and Rectangular Prisms

The 3 dimensions are called width, depth and height.

A three dimensional (3D) object.









The Surface Area here = (1+2)+(3+4)+(5)+(6)= WL + WH + WL + WH + HL + HL = 2WL + 2WH + 2HL

- 1) Find the surface area of a rectangle prism with a length of 6 cm, a width of 5 cm, and a height of 10 cm. (2 * 6) + (2 * 5) + (2 * 10) = 42
- 2 Find the surface area with a length of $\frac{1}{2}$ cm, a width of 8 cm, and a height of $\frac{1}{4}$ cm.

(2*1/2)+(2*8)+(2*1/4)=17.5



from a given point (the center).

Diameter

The radius is the distance from the center of the circle to its edge. The diameter of a circle is a segment whose end points lie on the circle and whose midpoint is the center of the circle and when someone says that something "lies on the circle" that means it's on the outline that traces the circle.

Diameter = ABRadius = CA, CB, CD

• How many diameter do we have in a circle?

• How many radii can we draw in a circle?

The distance around a circle is called circumference = $2r\pi$ or πr When r = radius, diameter = 2r.





A Circle is: It is the set of all points in a plane that are at an equal distance



Center





Examples

1) Find the circumference of a circle whose r = 4 cm. Circumference = $2 \pi r = 2(4) \pi = 8 \pi cm$

2) Find the circumference of a circle whose r = 3 cm, $\pi = \frac{22}{7}$ Circumference = $2 \pi r$ $= 2(3)(\frac{22}{2})$

$$=\left(\frac{132}{7}\right)^{\prime}$$

= 18.85 cm

The value of π is 22 or 3.14 $\pi = \frac{\text{Circumference}}{\text{Diameter}}$ or Circumference = π x Diameter

The area of a circle is the number of square units inside that circle A = π I²

Exercises

- 1 The radius of a circle is 3 inches, what is the area? π = 3.14 π r² = 28.26
- The diameter of a circle is 8 cm, what is the area? π r² = 50.24 2
- 78.5/3.14 = √25 3 The area a circle is 78.5 square meters, what is the radius?
- $2\pi r = 18.28/2 = 9.14/3.14 = 2.91$ 4 The circumference of a circle is 18.28 m, what is the area? area = πr^2 = 26.58
- (5) The area of a coin is 3.14 square centimeters, what is the radius and circumference of the circle? $\pi r^2 = 3.14/\pi$ Circumference = $2\pi r = 6.28$ r = 1



Probability and Statistics

7.1

Probability is a branch of mathematics that is concerned with the analysis of random phenomena. The outcome of a random event cannot by determined before it occurs, but it may be any of several possible outcomes. The actual outcome is to be determined by chance.

Statistics is a branch of mathematics dealing with the collection, analysis interpretation, presentation and organization of data like this table.

Α	В	С
23	45	30 - 10
70	33	20 - 39
100	45	

If you have 3 shirts: the first is blue, the second is red, and the third is orange, and you have 4 pairs of pants: black, white, green, and yellow. How many outfits do you have? Can you count them?

That means $3 \times 4 = 12$ different outfits.











The Basic Counting Principle







Exercise

Lee is planning an activity with his wife. He plans to watch a movie, go out for dinner, and then attend a sporting event. He is deciding between 5 movies, 8 restaurants, and 2 sporting events. How many different activities can Lee plan? 5 * 8 * 2 = 80

- 3 The probability to get a black ball is =





Each outcome has 1 out of 4 chances of happening, so each outcome is







n	Tue	Wed	Thu	Fri		
	14	10	20	5		
<u>m of no. of packets</u> No. of days 18 + 16 + 14 + 10 + 20 + 5						

Weighted Average

An average resulting from the multiplication of each component by a factor reflecting importance. In calculating an average involving several augntities, it is often seen that the value of one affects the answer more than the value of the others. This type of average is called 'weighted average'.

Examples

Three pencils were bought for \$2 each and 9 pencils were bought for \$6 each. What is the average price per pencil?

 $= (2 \times 3) = 6$

= 6 + 54

= 60

 $=\frac{60}{12}$

= \$5

 $= (9 \times 6) = 54$

Total price

Number of pencils

Price of 3 pencils \$2 each Price of 9 pencils \$6 each Price of (3+9) 12 pencils

Average price per pencil

Average price per pencil

This is not the average of \$2 and \$6. Since fewer pencils were bought for \$2 each than for \$6 each, the first price has less effect on the average than the second. This is an example of weighted average because it is necessary to attach more importance or weight to one price than the other.

A motorist drives 3 hours at 50 km/hr and 2 hours at 45 km/hr. Find his average speed for the whole journey.

Distance covered in 3 hours at 50 km/hr = $50 \times 3 = 150$ km Distance covered in 2 hours at 45 km/hr = $45 \times 2 = 90 \text{ km}$ Total distance covered in (3+2) 5 hours = 240 km

Average Speed

Average Speed

Total time taken = 240 $= \frac{5}{40}$ km/hr

_ Total distance covered

Median and Mode

Median

7.4

Is the middle value between the minimum and the maximum value of data arranged regularly.

Then the median of a set of data is the middle number when the data are listed in order form least to greatest.

Examples

- Find the median for 2.4.6. The median is `4'.
- the values are arranged in ascending order.
- The median for an even number of values is the mean of the two middle values when the values are arranged in ascending order.
- 60, 91, 65, and 50. Find the median. have an odd number of marks, the median is the middle score (65).
- the median.

We arrange marks in ascending order: 20, 50, 60, 65, 70, 75, 84, 91, 92, 95. Since we have an even number of marks, the median is the mean of the two middle marks. The two middle marks are 70 and 75.





• The median for an odd number of values is the middle number when

Seven students from a class participated in a guiz. Their marks were 20, 84, 95,

We arrange the marks in ascending order of 20, 50, 60, 65, 84, 91, 95. Since we

3 Suppose, 3 more students from the same class participated in the same guiz, as in the above example, and their marks were 70, 75, and 92. Find

> = 70 + 75The median The median = 72.5

Exercises



- (a) 3, 2, 0, 4, 9 $0, 2, 3, 4, 9 \rightarrow 3$
- **(b)** 11, 8, 10, 9, 2, 3, 1, 4 1, 2, 3, 4, 8, 9, 10, $11 \rightarrow 4 + 8/2 = 6$
- (c) 90, 100, 89, 70, 85, 101 70, 85, 89, 90, 100, $101 \rightarrow 90 + 89/2 = 89.5$

Find the median cut score, then find the average.

2 During the first marking period, Sara's math cut scores were 90, 91, 92, 88, 97, 87.

87.88.90.91.92.97 median = 90 + 91/2 = 90.5avg = 90.83

Mode

The most frequently occurring number in a data set is called 'mode'. It is often useful to know the number which occurs most frequently in a set of numbers.

The marks obtained by a student in a series of tests are given as follows: 20, 18, 15, 18, 16, 18, 17. The modal mark or the mode of the marks is 18 since it appeared most often.

Exercises

- 1) Find the average, median and mode of the following numbers. Mode = 7Mode = 1110, 11, 13, 11, 15, 16 Avg = 12.66 **a** 11, 9, 10, 7, 6, 5, 8, 7 **(a)** Avg = 7.87 Median = 7.5 Median = 122 The scores of a basketball team in a series of matches are: 63, 63, 75, 67, 68, 52, 50, 63, 56, 52. 50, 52, 52, 56, 63, 63, 63, 67, 68, 75 (a) Find the average **b** Determine the C What is the modal score of the matches. median score. score of the matches?
- 3 The following is the number of problems that teacher Lee assigned for homework in 10 different days. Find the mode of the following numbers: 8, 11, 9, 14, 13, 18, 6, 9, 10, 13, 14, 9, 6, 12, 13, 16, 14 mode = 9, 13, 14

Note : Speed = $\frac{\text{Distance}}{\text{Time}}$, Distance = Speed x Time

- 1) The average age of 16 boys is 15 years and of 24 girls is 10 years. Find the average age of all. $\frac{15+10}{2} = 12.5$
- 2 30 kg of coal costing \$8 per kg is mixed with 10 kg of coal costing \$6 per kg. Find the average per kg. \$7
- 3 The average score of 8 matches in one day was 230, and that of 12 matches was 200, find the average of all. 215





